

**fischer**<sup>11,40</sup>

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fischer{$x:ut2,
         $try:ut2,
         $taken:ut2,
         $contending:ut2,
         $free:ut2,
         $mine:ut2,
         $wanted:ut2,
         $z:ut2}
         (es; L)
 $\equiv_{\text{def}}$   $\forall e:\text{es-E}(es).$ 
 $(\text{loc}(e) \in L)$ 
 $\Rightarrow (\text{es-dtype}(es; \text{loc}(e); \text{mkid}\{\$x:ut2\}; \text{Id})$ 
 $c \wedge (((\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$free:ut2\})$ 
 $\vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$taken:ut2\})$ 
 $\vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$mine:ut2\})$ 
 $\vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$try:ut2\})$ 
 $\vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$contending:ut2\}))$ 
 $\wedge (\text{es-initially}(es; \text{loc}(e); \text{mkid}\{\$x:ut2\}) = \text{mkid}\{\$free:ut2\})$ 
 $\wedge (@e(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$try:ut2\})$ 
 $\Rightarrow (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$free:ut2\})$ 
 $\vee (\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$contending:ut2\}))$ 
 $\wedge \text{l_all}(L;$ 
 $\text{Id};$ 
 $i.((\neg(i = \text{loc}(e)))$ 
 $\Rightarrow (e \text{ sends on } <\text{loc}(e)$ 
 $, i$ 
 $, \text{mkid}\{\$z:ut2\} > \text{with tag } \text{mkid}\{\$wanted:ut2\}))))))$ 
 $\wedge (@e(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$mine:ut2\})$ 
 $\Rightarrow (\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$try:ut2\}))$ 
 $\wedge (@e(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$free:ut2\})$ 
 $\iff (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$taken:ut2\})$ 
 $\wedge ((\text{es-isrcv}(es; e))$ 
 $c \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$free:ut2\})$ 
 $\wedge (\exists i:\text{Id}$ 
 $((i \in L)$ 
 $\wedge (\neg(i = \text{loc}(e)))$ 
 $\wedge (\text{es-lnk}(es; e) = <i, \text{loc}(e), \text{mkid}\{\$z:ut2\} >))))))$ 
 $\vee ((\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$mine:ut2\})$ 
 $\wedge \text{l_all}(L;$ 
 $\text{Id};$ 
 $i.((\neg(i = \text{loc}(e)))$ 
 $\Rightarrow (e \text{ sends on } <\text{loc}(e)$ 

```

$$\begin{aligned}
& , i \\
& , \text{mkid}\{\$z:ut2\} > \text{with tag } \text{mkid}\{\$free:ut2\})))))) \\
\wedge (@e(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$contending:ut2\})) \\
\iff & ((\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$try:ut2\}) \\
& \wedge ((\uparrow \text{es-isrcv}(es; e)) \\
& \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\}) \\
& \wedge (\exists i:\text{Id} \\
& \quad ((i \in L) \\
& \quad \wedge (\neg(i = \text{loc}(e))) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{loc}(e), \text{mkid}\{\$z:ut2\} \rangle)))))) \\
\wedge (@e(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$taken:ut2\})) \\
\Rightarrow & (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$contending:ut2\}) \\
& \vee (\text{es-when}(es; \text{mkid}\{\$x:ut2\}; e) = \text{mkid}\{\$free:ut2\})) \\
& \wedge ((\uparrow \text{es-isrcv}(es; e)) \\
& \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\}) \\
& \wedge (\exists i:\text{Id} \\
& \quad ((i \in L) \\
& \quad \wedge (\neg(i = \text{loc}(e))) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{loc}(e), \text{mkid}\{\$z:ut2\} \rangle)))))) \\
\wedge ((\uparrow \text{es-isrcv}(es; e)) \\
\Rightarrow & (\text{es-tag}(es; e) = \text{mkid}\{\$free:ut2\}) \\
\Rightarrow & (\exists i:\text{Id} \\
& \quad ((i \in L) \\
& \quad \wedge (\neg(i = \text{loc}(e))) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{loc}(e), \text{mkid}\{\$z:ut2\} \rangle))) \\
\Rightarrow & (\text{subtype\_rel}(\text{es-vartype}(es; \text{loc}(\text{es-sender}(es; e)); \text{mkid}\{\$x:ut2\}); \text{Id}) \\
& \wedge (@\text{es-sender}(es; e)(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$free:ut2\}) \\
& \quad \wedge (\text{es-when}(es; \text{mkid}\{\$x:ut2\}; \text{es-sender}(es; e)) = \text{mkid}\{\$mine:ut2\}))) \\
\wedge ((\uparrow \text{es-isrcv}(es; e)) \\
\Rightarrow & (\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\}) \\
\Rightarrow & (\exists i:\text{Id} \\
& \quad ((i \in L) \\
& \quad \wedge (\neg(i = \text{loc}(e))) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{loc}(e), \text{mkid}\{\$z:ut2\} \rangle))) \\
\Rightarrow & (\text{subtype\_rel}(\text{es-vartype}(es; \text{loc}(\text{es-sender}(es; e)); \text{mkid}\{\$x:ut2\}); \text{Id}) \\
& \wedge @\text{es-sender}(es; e)(\text{mkid}\{\$x:ut2\} \rightarrow \text{mkid}\{\$try:ut2\})))
\end{aligned}$$

*clarification:*

```
fischer{\$x:ut2,
\$try:ut2,
\$taken:ut2,
\$contending:ut2,
\$free:ut2,
\$mine:ut2,
\$wanted:ut2,
```

$$\begin{aligned}
& \$z:ut2\} \\
& (es; L) \\
\equiv_{\text{def}} & \forall e:es \cdot E(es). \\
& (\text{es-loc}(es; e) \in L \in \text{Id}) \\
\Rightarrow & (\text{es-dtype}(es; \text{es-loc}(es; e); \text{mkid}\{\$x:ut2\}; \text{Id}) \\
& \quad c \wedge (((\text{es-after}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$free:ut2\} \in \text{Id}) \\
& \quad \quad \vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$taken:ut2\} \in \text{Id}) \\
& \quad \quad \vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$mine:ut2\} \in \text{Id}) \\
& \quad \quad \vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$try:ut2\} \in \text{Id}) \\
& \quad \quad \vee (\text{es-after}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$contending:ut2\} \in \text{Id})) \\
& \wedge (\text{es-initially}(es; \text{es-loc}(es; e); \text{mkid}\{\$x:ut2\}) = \text{mkid}\{\$free:ut2\} \in \text{Id}) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:ut2\}; e; \text{mkid}\{\$try:ut2\}) \\
\Rightarrow & (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$free:ut2\} \in \text{Id}) \\
& \quad \vee (\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$contending:ut2\} \in \text{Id})) \\
& \wedge \text{l\_all}(L; \\
& \quad \text{Id}; \\
& \quad i.((\neg(i = \text{es-loc}(es; e)) \in \text{Id})) \\
\Rightarrow & \text{es-sends-on}(es; e; <\text{es-loc}(es; e) \\
& \quad , i \\
& \quad , \text{mkid}\{\$z:ut2\} >; \text{mkid}\{\$wanted:ut2\})))) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:ut2\}; e; \text{mkid}\{\$mine:ut2\}) \\
\Rightarrow & (\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$try:ut2\} \in \text{Id})) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:ut2\}; e; \text{mkid}\{\$free:ut2\}) \\
\iff & (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$taken:ut2\} \in \text{Id}) \\
& \quad \wedge ((\uparrow \text{es-isrcv}(es; e))) \\
& \quad c \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$free:ut2\} \in \text{Id}) \\
& \quad \wedge (\exists i:\text{Id} \\
& \quad \quad ((i \in L \in \text{Id}) \\
& \quad \quad \wedge (\neg(i = \text{es-loc}(es; e)) \in \text{Id}) \\
& \quad \quad \wedge (\text{es-lnk}(es; e) \\
& \quad \quad = \\
& \quad \quad <i, \text{es-loc}(es; e), \text{mkid}\{\$z:ut2\} > \\
& \quad \quad \in \text{IdLnk})))))) \\
& \vee ((\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$mine:ut2\} \in \text{Id}) \\
& \wedge \text{l\_all}(L; \\
& \quad \text{Id}; \\
& \quad i.((\neg(i = \text{es-loc}(es; e)) \in \text{Id})) \\
\Rightarrow & \text{es-sends-on}(es; e; <\text{es-loc}(es; e) \\
& \quad , i \\
& \quad , \text{mkid}\{\$z:ut2\} >; \text{mkid}\{\$free:ut2\})))) \\
& \wedge (\text{es-change-to}(es; \text{Id}; \text{mkid}\{\$x:ut2\}; e; \text{mkid}\{\$contending:ut2\}) \\
\iff & ((\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$try:ut2\} \in \text{Id}) \\
& \quad \wedge ((\uparrow \text{es-isrcv}(es; e))) \\
& \quad c \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\} \in \text{Id}) \\
& \quad \wedge (\exists i:\text{Id} \\
& \quad \quad ((i \in L \in \text{Id})
\end{aligned}$$

$$\begin{aligned}
& \wedge (\neg(i = \text{es-loc}(es; e) \in \text{Id})) \\
& \wedge (\text{es-lnk}(es; e)) \\
& = \\
& \quad \langle i, \text{es-loc}(es; e), \text{mkid}\{\$z:ut2\} \rangle \\
& \quad \in \text{IdLnk}))))))) \\
& \wedge (\text{es-change-to}(es;\text{Id};\text{mkid}\{\$x:ut2\};e;\text{mkid}\{\$taken:ut2\}) \\
& \Rightarrow (((\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$contending:ut2\} \in \text{Id}) \\
& \vee (\text{es-when}(es; \text{mkid}\{\$x:ut2\}); e) = \text{mkid}\{\$free:ut2\} \in \text{Id})) \\
& \wedge ((\uparrow \text{es-isrcv}(es; e)) \\
& \quad c \wedge ((\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\} \in \text{Id}) \\
& \quad \wedge (\exists i:\text{Id} \\
& \quad \quad ((i \in L \in \text{Id}) \\
& \quad \quad \wedge (\neg(i = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \quad \wedge (\text{es-lnk}(es; e)) \\
& \quad \quad = \\
& \quad \quad \langle i, \text{es-loc}(es; e), \text{mkid}\{\$z:ut2\} \rangle \\
& \quad \quad \in \text{IdLnk}))))))) \\
& \wedge ((\uparrow \text{es-isrcv}(es; e)) \\
& \Rightarrow (\text{es-tag}(es; e) = \text{mkid}\{\$free:ut2\} \in \text{Id}) \\
& \Rightarrow (\exists i:\text{Id} \\
& \quad ((i \in L \in \text{Id}) \\
& \quad \wedge (\neg(i = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{es-loc}(es; e), \text{mkid}\{\$z:ut2\} \rangle \in \text{IdLnk}))) \\
& \Rightarrow (\text{subtype\_rel}(\text{es-vartype}(es; \text{es-loc}(es; \text{es-sender}(es; e)); \text{mkid}\{\$x:ut2\}); \\
& \quad \text{Id}) \\
& \quad c \wedge (\text{es-change-to}(es;\text{Id};\text{mkid}\{\$x:ut2\};\text{es-sender}(es; e);\text{mkid}\{\$free:ut2\}) \\
& \quad \wedge (\text{es-when}(es; \text{mkid}\{\$x:ut2\}; \text{es-sender}(es; e)) \\
& \quad = \\
& \quad \text{mkid}\{\$mine:ut2\} \\
& \quad \in \text{Id})))) \\
& \wedge ((\uparrow \text{es-isrcv}(es; e)) \\
& \Rightarrow (\text{es-tag}(es; e) = \text{mkid}\{\$wanted:ut2\} \in \text{Id}) \\
& \Rightarrow (\exists i:\text{Id} \\
& \quad ((i \in L \in \text{Id}) \\
& \quad \wedge (\neg(i = \text{es-loc}(es; e) \in \text{Id})) \\
& \quad \wedge (\text{es-lnk}(es; e) = \langle i, \text{es-loc}(es; e), \text{mkid}\{\$z:ut2\} \rangle \in \text{IdLnk}))) \\
& \Rightarrow (\text{subtype\_rel}(\text{es-vartype}(es; \text{es-loc}(es; \text{es-sender}(es; e)); \text{mkid}\{\$x:ut2\}); \\
& \quad \text{Id}) \\
& \quad c \wedge \text{es-change-to}(es;\text{Id};\text{mkid}\{\$x:ut2\};\text{es-sender}(es; e);\text{mkid}\{\$try:ut2\})))) \\
\end{aligned}$$